



Impact of HWP non-idealities on the observed CMB polarization

Marta Monelli

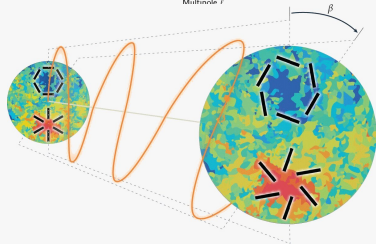
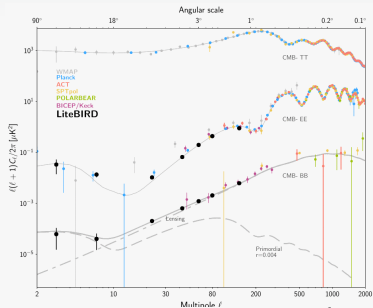
Kavli IPMU

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new physics from CMB polarization

- ▶ B modes are sensitive to primordial GWs ($C_{\ell}^{BB} = rC_{\ell}^{\text{GW}} + C_{\ell}^{\text{lensing}}$): they can be used to test/constrain **inflationary models**.

- ▶ CMB polarization is also sensitive to cosmic birefringence: probe of **parity-violating** physics.



how to get there

- LiteBIRD,
- Simons Observatory,
- South Pole Observatory,
- CMB-S4,
- ...

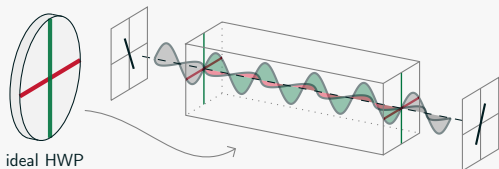
Mitigating systematics is key!

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Mitigating systematics is key!

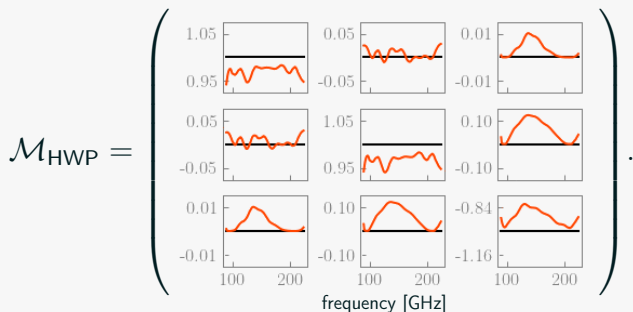
Some instruments will employ rotating **half-wave plates (HWPs)** as polarization modulators to mitigate $1/f$ noise and reduce $I \rightarrow P$ leakage.



$$\mathcal{M}_{\text{ideal}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

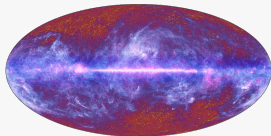
beyond the ideal HWP

For a realistic HWP, $\mathcal{M}_{\text{HWP}} \neq \text{diag}(1, 1, -1)$. Instead



How does this affect the observed maps/spectra/...?

two complementary approaches



detection

time ordered data (TOD)

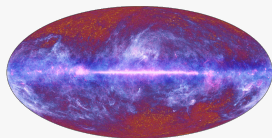
map-making

multi-frequency maps

foreground cleaning

CMB sky maps

two complementary approaches



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time ordered data (TOD)

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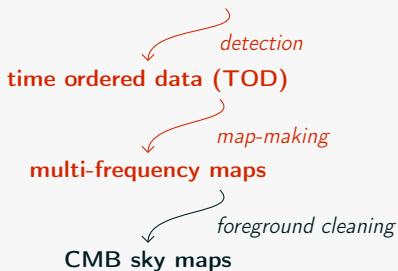
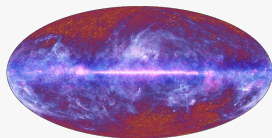
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CMB sky maps

TOD simulations are key to study systematics: they can account for them in their (at least partial) complexity.

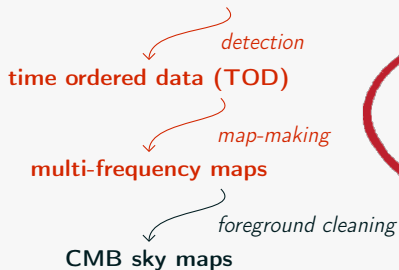
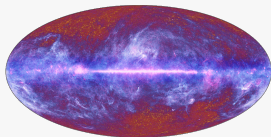
two complementary approaches



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Map-based simulations are approximate but extremely useful to gain some intuition about the problem at hand.

two complementary approaches



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modeling the observed maps

TOD: $d = A m_{in}$

map-maker: $m_{out} = (\hat{A}^T \hat{A})^{-1} \hat{A}^T d$

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recalling the structure of response matrices

explicitly: $m_{out,p} = \left[\sum_{j't' \in \{jt\}_p} \hat{S}_{j't'} \hat{S}_{j't'}^T \right]^{-1} \left[\sum_{jt \in \{jt\}_p} \hat{S}_{jt} S_{jt}^T \right] m_{in,p}$

S_{jt} encodes instrumental response relative to detector j at time t .

validation: toy model

$$m_{\text{out},p} = \left[\sum_{j't' \in \{jt\}_p} \widehat{\mathbb{S}}_{j't'} \widehat{\mathbb{S}}_{j't'}^T \right]^{-1} \left[\sum_{jt \in \{jt\}_p} \widehat{\mathbb{S}}_{jt} \mathbb{S}_{jt}^T \right] m_{\text{in},p}$$

- ▶ no noise,
- ▶ single frequency,
- ▶ CMB-only,
- ▶ ideal binning map-maker,
- ▶ neglecting non-linearities,
- ▶ simple beams,
- ▶ HWP aligned to the detector line of sight.

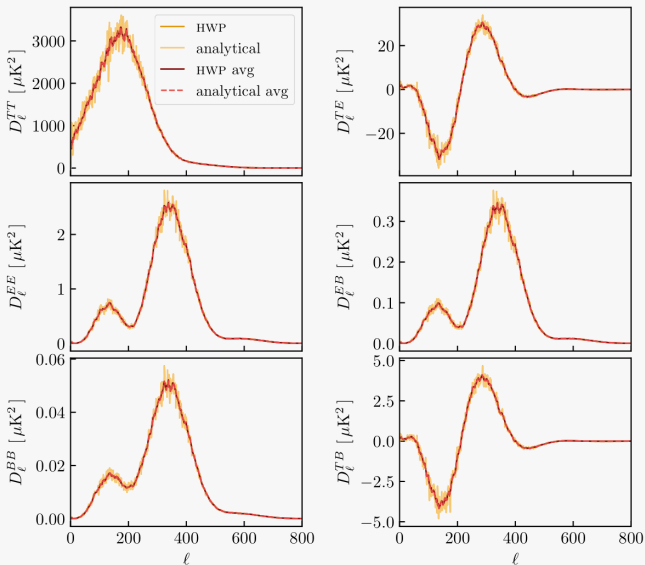
validation: toy model

$$\begin{aligned}I_{\text{out}} &= m_{ii}I_{\text{in}} + (m_{iq}Q_{\text{in}} + m_{iu}U_{\text{in}})\cos(2\alpha) + (m_{iq}U_{\text{in}} - m_{iu}Q_{\text{in}})\sin(2\alpha) \\Q_{\text{out}} &= \frac{1}{2}\left\{(m_{qq} - m_{uu})Q_{\text{in}} + (m_{qu} + m_{uq})U_{\text{in}} + 2m_{qi}I_{\text{in}}\cos(2\alpha) + 2m_{ui}I_{\text{in}}\sin(2\alpha)\right. \\&\quad + [(m_{qq} + m_{uu})Q_{\text{in}} + (m_{qu} - m_{uq})U_{\text{in}}]\cos(4\alpha) \\&\quad \left. + [-(m_{qu} - m_{uq})Q_{\text{in}} + (m_{qq} + m_{uu})U_{\text{in}}]\sin(4\alpha)\right\} \\U_{\text{out}} &= \frac{1}{2}\left\{(m_{qq} - m_{uu})U_{\text{in}} - (m_{qu} + m_{uq})Q_{\text{in}} - 2m_{ui}I_{\text{in}}\cos(2\alpha) + 2m_{qi}I_{\text{in}}\sin(2\alpha)\right. \\&\quad + [-(m_{qq} + m_{uu})U_{\text{in}} + (m_{qu} - m_{uq})Q_{\text{in}}]\cos(4\alpha) \\&\quad \left. + [(m_{qu} - m_{uq})U_{\text{in}} + (m_{qq} + m_{uu})Q_{\text{in}}]\sin(4\alpha)\right\} \quad \text{where } \alpha \equiv \phi + \psi\end{aligned}$$

For **good coverage** and **rapidly spinning HWP**:

$$m_{\text{out},p} \simeq \begin{pmatrix} m_{ii} & 0 & 0 \\ 0 & (m_{qq} - m_{uu})/2 & (m_{qu} + m_{uq})/2 \\ 0 & -(m_{qu} + m_{uq})/2 & (m_{qq} - m_{uu})/2 \end{pmatrix} m_{\text{in},p}.$$

validation: toy model



relaxing some assumptions

$$m_{\text{out},p} = \left[\sum_{j't' \in \{jt\}_p} \widehat{\mathbb{S}}_{j't'} \widehat{\mathbb{S}}_{j't'}^T \right]^{-1} \left[\sum_{jt \in \{jt\}_p} \widehat{\mathbb{S}}_{jt} \mathbb{S}_{jt}^T \right] m_{\text{in},p}$$

- ▶ ~~no noise,~~
- ▶ ~~single frequency,~~
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band-integrated maps

$$\text{with HWP: } m_{\text{out}}^i \simeq \sum_{\lambda} \begin{pmatrix} g_{\lambda}^i & 0 & 0 \\ 0 & \rho_{\lambda}^i & \eta_{\lambda}^i \\ 0 & -\eta_{\lambda}^i & \rho_{\lambda}^i \end{pmatrix} \bar{m}_{\lambda}^i(\nu_*) + n^i,$$

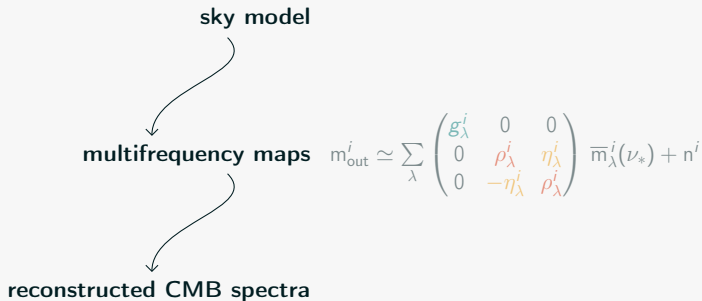
$$\text{where } g_{\lambda}^i \equiv \int_{\nu_{\min}^i}^{\nu_{\max}^i} \frac{d\nu}{\Delta\nu^i} a_{\lambda}(\nu) m_{\text{ii}}(\nu),$$

$$\rho_{\lambda}^i \equiv \frac{1}{2} \int_{\nu_{\min}^i}^{\nu_{\max}^i} \frac{d\nu}{\Delta\nu^i} a_{\lambda}(\nu) [m_{\text{qq}}(\nu) - m_{\text{uu}}(\nu)],$$

$$\eta_{\lambda}^i \equiv \frac{1}{2} \int_{\nu_{\min}^i}^{\nu_{\max}^i} \frac{d\nu}{\Delta\nu^i} a_{\lambda}(\nu) [m_{\text{qu}}(\nu) + m_{\text{uq}}(\nu)].$$

How the HWP non-idealities affect **gain**, **polarization-efficiency** and **cross-pol leakage**, differ for each frequency channel and each component.

an extra step: end-to-end model



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sky model CMB, dust, synchrotron; uniform SEDs

multifrequency maps

$$m_{\text{out}}^i \simeq \sum_{\lambda} \begin{pmatrix} g_{\lambda}^i & 0 & 0 \\ 0 & \rho_{\lambda}^i & \eta_{\lambda}^i \\ 0 & -\eta_{\lambda}^i & \rho_{\lambda}^i \end{pmatrix} \bar{m}_{\lambda}^i(\nu_*) + n^i$$

reconstructed CMB spectra

an extra step: end-to-end model

sky model CMB, dust, synchrotron; **uniform SEDs**

multifrequency maps $m_{\text{out}}^i \simeq \sum_{\lambda} \begin{pmatrix} g_{\lambda}^i & 0 & 0 \\ 0 & \rho_{\lambda}^i & \eta_{\lambda}^i \\ 0 & -\eta_{\lambda}^i & \rho_{\lambda}^i \end{pmatrix} \bar{m}_{\lambda}^i(\nu_*) + n^i$

HILC foreground removal

reconstructed CMB spectra

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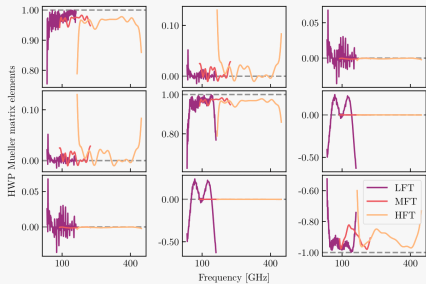
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HILC foreground removal

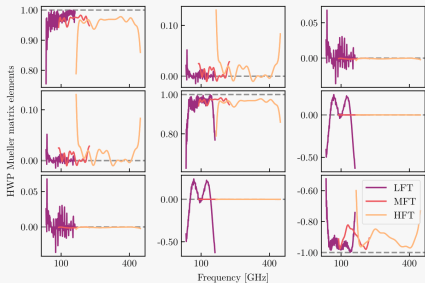
reconstructed CMB spectra **can be modeled analytically!**

$$C_{\ell, \text{HILC}}^{BB} = \sum_{i,j=1}^{n_{\text{chan}}} \frac{w_{\ell}^i w_{\ell}^j}{g_{\text{CMB}}^i g_{\text{CMB}}^j} \left\{ \sum_{\lambda} \left[\rho_{\lambda}^i \rho_{\lambda}^j C_{\ell, \lambda}^{BB} + \eta_{\lambda}^i \eta_{\lambda}^j C_{\ell, \lambda}^{EE} - (\rho_{\lambda}^i \eta_{\lambda}^j + \eta_{\lambda}^i \rho_{\lambda}^j) C_{\ell, \lambda}^{EB} \right] + \frac{N_{\ell}^{BB, ij}}{B_{\ell}^i B_{\ell}^j} \right\}$$

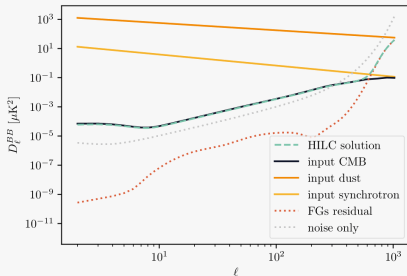
HILC solution



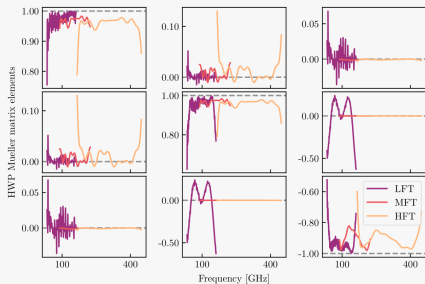
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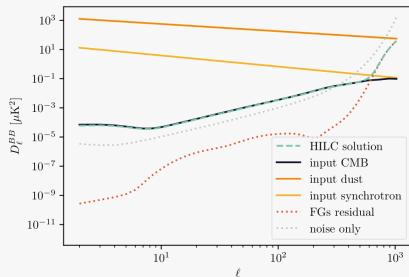
(power law $D_{\ell,\lambda}$)



HILC solution

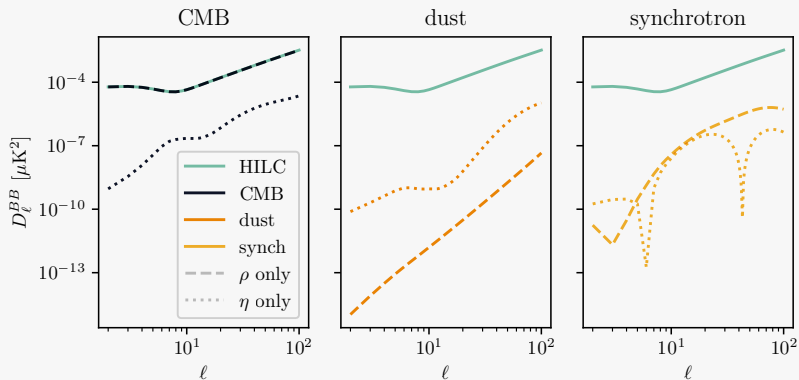


(power law $D_{\ell,\lambda}$)



Blind component separation reduces the impact of the non-idealities.
We are left with a slight **underestimation** of r .

term by term

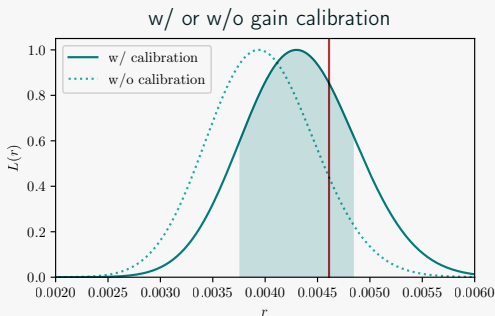


$$C_{\ell, \text{HILC}}^{BB} = \sum_{i,j=1}^{n_{\text{chan}}} \frac{w_{\ell}^i w_{\ell}^j}{g_{\text{CMB}}^i g_{\text{CMB}}^j} \left\{ \sum_{\lambda} \left[\rho_{\lambda}^i \rho_{\lambda}^j C_{\ell, \lambda}^{BB} + \eta_{\lambda}^i \eta_{\lambda}^j C_{\ell, \lambda}^{EE} - (\rho_{\lambda}^i \eta_{\lambda}^j + \eta_{\lambda}^i \rho_{\lambda}^j) C_{\ell, \lambda}^{EB} \right] + \frac{N_{\ell}^{BB, ij}}{B_{\ell}^i B_{\ell}^j} \right\}$$

impact on r and design recommendations

To mitigate this effect, one can **design** the HWP to maximize the benefits of gain calibration.

- ▷ Cross-polarization coupling should be small, $\zeta_{1,2} \leq 10^{-2}$, which can be achieved for both metal-mesh and multi-layer HWPs;
- ▷ The loss parameters should also be small, $h_{1,2} \leq 10^{-2}$, or, alternatively, $|h_1 - h_2| \leq 10^{-3}$;
- ▷ At least one of $h_1(\nu) + h_2(\nu)$ and $[1 + \cos \beta(\nu)]/2$ should be slowly varying within the band, so that $\rho_{\text{CMB}}^i \approx A^i g_{\text{CMB}}^i$;
- ▷ Cross-polarization coupling can be kept under control by requiring $\zeta_{1,2}$ to be even smaller, or alternatively, by ensuring that η_{CMB}^i fluctuates around zero.



conclusions

- ▶ CMB polarization is a promising probe of new physics, that can only be extracted if systematics are well under control,
- ▶ A rotating HWP can help, but it induces **additional systematics** which should be accounted for.
- ▶ Map-based simulations can help us gain intuition about the problem and develop mitigation strategies (**design recommendations**).
- ▶ **Next steps**: consider realistic sky models, together with a sophisticated foreground cleaning method: the multi-clustering needlet internal linear combination (MCNILC). Do the design recommendation change?